

THERMODYNAMIC QUANTITIES FOR THE IONIZATION REACTIONS OF BUFFERS IN WATER

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This table contains selected values for the pK , standard molar enthalpy of reaction $\Delta_r H^\circ$, and standard molar heat-capacity change $\Delta_r C_p^\circ$ for the ionization reactions of 64 buffers many of which are relevant to biochemistry and to biology.¹ The values pertain to the temperature $T = 298.15$ K and the pressure $p = 0.1$ MPa. The standard state is the hypothetical ideal solution of unit molality. These data permit one to calculate values of the pK and of $\Delta_r H^\circ$ at temperatures in the vicinity $\{T \approx (274\text{ K to }350\text{ K})\}$ of the reference temperature $\theta = 298.15$ K by using the following equations²

$$\Delta_r G_T^\circ = -RT \ln K_T = \ln(10) \cdot RT \cdot pK_T, \quad (1)$$

$$R \ln K_T = -(\Delta_r G_\theta^\circ / \theta) + \Delta_r H_\theta^\circ \{1/\theta\} - \{1/T\} + \Delta_r C_{p\theta}^\circ \{(\theta/T) - 1 + \ln(T/\theta)\}, \quad (2)$$

$$\Delta_r H_T^\circ = \Delta_r H_\theta^\circ + \Delta_r C_{p\theta}^\circ (T - \theta). \quad (3)$$

Here, $\Delta_r G^\circ$ is the standard molar Gibbs energy change and K is the equilibrium constant for a reaction; R is the gas constant ($8.314 \text{ J K}^{-1} \text{ mol}^{-1}$). The subscripts T and θ denote the temperature to which a quantity pertains, the subscript p denotes constant pres-

sure, and the subscript r denotes that the quantity refers to a reaction. Combination of equations (1) and (2) yields the following equation that gives pK as a function of temperature:

$$pK_T = -\{R \cdot \ln(10)\}^{-1} [-\{\ln(10) \cdot RT \cdot pK_\theta / \theta\} + \Delta_r H_\theta^\circ \{1/\theta\} - \{1/T\} + \Delta_r C_{p\theta}^\circ \{(\theta/T) - 1 + \ln(T/\theta)\}]. \quad (4)$$

The above equations neglect higher order terms that involve temperature derivatives of $\Delta_r C_p^\circ$. Also, it is important to recognize that the values of pK and $\Delta_r H^\circ$ effectively pertain to ionic strength $I = 0$. However, the values of pK and $\Delta_r H^\circ$ are almost always dependent on the ionic strength and the actual composition of the solution. These issues are discussed in Reference 1 which also gives an approximate method for making appropriate corrections.

References

- Goldberg, R. N., Kishore, N., and Lennen, R. M., "Thermodynamic Quantities for the Ionization Reactions of Buffers," *J. Phys. Chem. Ref. Data*, in press.
- Clarke, E. C. W., and Glew, D. N., *Trans. Faraday Soc.*, 62, 539-547, 1966.

Selected Values of Thermodynamic Quantities for the Ionization Reactions of Buffers in Water at $T = 298.15$ K and $p = 0.1$ MPa

Buffer	Reaction	pK	$\Delta_r H^\circ$	$\Delta_r C_p^\circ$
			kJ mol^{-1}	$\text{J K}^{-1} \text{ mol}^{-1}$
ACES	$\text{HL}^\pm = \text{H}^+ + \text{L}^-$, ($\text{HL} = \text{C}_4\text{H}_{10}\text{N}_2\text{O}_4\text{S}$)	6.847	30.43	-49
Acetate	$\text{HL} = \text{H}^+ + \text{L}^-$, ($\text{HL} = \text{C}_2\text{H}_4\text{O}_2$)	4.756	-0.41	-142
ADA	$\text{H}_3\text{L}^\pm = \text{H}^+ + \text{H}_2\text{L}^\pm$, ($\text{H}_2\text{L} = \text{C}_6\text{H}_{10}\text{N}_2\text{O}_5$)	1.59		
	$\text{H}_2\text{L}^\pm = \text{H}^+ + \text{HL}^-$	2.48	16.7	
	$\text{HL}^- = \text{H}^+ + \text{L}^{2-}$	6.844	12.23	-144
2-Amino-2-methyl-1,3-propanediol	$\text{HL}^\pm = \text{H}^+ + \text{L}$, ($\text{L} = \text{C}_4\text{H}_{11}\text{NO}_2$)	8.801	49.85	-44
2-Amino-2-methyl-1-propanol	$\text{HL}^\pm = \text{H}^+ + \text{L}$, ($\text{L} = \text{C}_4\text{H}_{11}\text{NO}$)	9.694	54.05	≈ -21
3-Amino-1-propanesulfonic acid	$\text{HL} = \text{H}^+ + \text{L}^-$, ($\text{HL} = \text{C}_3\text{H}_9\text{NO}_3\text{S}$)	10.2		
Ammonia	$\text{NH}_4^+ = \text{H}^+ + \text{NH}_3$	9.245	51.95	8
AMPSO	$\text{HL}^\pm = \text{H}^+ + \text{L}^-$, ($\text{HL} = \text{C}_7\text{H}_{17}\text{NO}_5\text{S}$)	9.138	43.19	-61
Arsenate	$\text{H}_3\text{AsO}_4 = \text{H}^+ + \text{H}_2\text{AsO}_4^-$	2.31	-7.8	
	$\text{H}_2\text{AsO}_4^- = \text{H}^+ + \text{HASO}_4^{2-}$	7.05	1.7	
	$\text{HASO}_4^{2-} = \text{H}^+ + \text{AsO}_4^{3-}$	11.9	15.9	
Barbital	$\text{H}_2\text{L} = \text{H}^+ + \text{HL}^-$, ($\text{H}_2\text{L} = \text{C}_8\text{H}_{12}\text{N}_2\text{O}_3$)	7.980	24.27	-135
	$\text{HL}^- = \text{H}^+ + \text{L}^{2-}$	12.8		
BES	$\text{HL}^\pm = \text{H}^+ + \text{L}^-$, ($\text{HL} = \text{C}_6\text{H}_{15}\text{NO}_5\text{S}$)	7.187	24.25	-2
Bicine	$\text{H}_2\text{L}^\pm = \text{H}^+ + \text{HL}^\pm$, ($\text{HL} = \text{C}_6\text{H}_{13}\text{NO}_4$)	2.0		
	$\text{HL}^\pm = \text{H}^+ + \text{L}^-$	8.334	26.34	0
Bis-tris	$\text{H}_3\text{L}^\pm = \text{H}^+ + \text{H}_2\text{L}^\pm$, ($\text{H}_2\text{L} = \text{C}_8\text{H}_{19}\text{NO}_5$)	6.484	28.4	27
Bis-tris propane	$\text{H}_2\text{L}^{2+} = \text{H}^+ + \text{HL}^+$, ($\text{L} = \text{C}_{11}\text{H}_{26}\text{N}_2\text{O}_6$)	6.65		
	$\text{HL}^+ = \text{H}^+ + \text{L}$	9.10		
Borate	$\text{H}_3\text{BO}_3 = \text{H}^+ + \text{H}_2\text{BO}_3^-$	9.237	13.8	≈ -240
Cacodylate	$\text{H}_2\text{L}^\pm = \text{H}^+ + \text{HL}$, ($\text{HL} = \text{C}_2\text{H}_6\text{AsO}_2$)	1.78	-3.5	
	$\text{HL} = \text{H}^+ + \text{L}^-$	6.28	-3.0	-86
CAPS	$\text{HL}^\pm = \text{H}^+ + \text{L}^-$, ($\text{HL} = \text{C}_9\text{H}_{19}\text{NO}_3\text{S}$)	10.499	48.1	57
CAPSO	$\text{HL}^\pm = \text{H}^+ + \text{L}^-$, ($\text{HL} = \text{C}_9\text{H}_{19}\text{NO}_4\text{S}$)	9.825	46.67	21
Carbonate	$\text{H}_2\text{CO}_3 = \text{H}^+ + \text{HCO}_3^-$	6.351	9.15	-371
	$\text{HCO}_3^- = \text{H}^+ + \text{CO}_3^{2-}$	10.329	14.70	-249
CHES	$\text{HL}^\pm = \text{H}^+ + \text{L}^-$, ($\text{HL} = \text{C}_8\text{H}_{17}\text{NO}_3\text{S}$)	9.394	39.55	9

Thermodynamic Quantities for the Ionization Reactions of Buffers in Water

Buffer	Reaction	pK	$\Delta_f H^\circ$ kJ mol ⁻¹	$\Delta_r C_p^\circ$ J K ⁻¹ mol ⁻¹
Citrate	$H_3L = H^+ + H_2L^-$, ($H_3L = C_6H_8O_7$)	3.128	4.07	-131
	$H_2L^- = H^+ + HL^{2-}$	4.761	2.23	-178
	$HL^{2-} = H^+ + L^{3-}$	6.396	-3.38	-254
L-Cysteine	$H_3L^+ = H^+ + H_2L$, ($H_2L = C_3H_7NO_2S$)	1.71	≈ -0.6	
	$H_2L = H^+ + HL^-$	8.36	36.1	≈ -66
	$HL^- = H^+ + L^{2-}$	10.75	34.1	≈ -204
Diethanolamine	$HL^+ = H^+ + L$, ($L = C_4H_{11}NO_2$)	8.883	42.08	36
Diglycolate	$H_2L = H^+ + HL^-$, ($H_2L = C_4H_6O_5$)	3.05	-0.1	≈ -142
	$HL^- = H^+ + L^{2-}$	4.37	-7.2	≈ -138
3,3-Dimethylglutarate	$H_2L = H^+ + HL^-$, ($H_2L = C_7H_{12}O_4$)	3.70		
	$HL^- = H^+ + L^{2-}$	6.34		
DIPSO	$HL^+ = H^+ + L^-$, ($HL = C_7H_{17}NO_6S$)	7.576	30.18	42
Ethanolamine	$HL^+ = H^+ + L$, ($L = C_2H_7NO$)	9.498	50.52	26
N-Ethylmorpholine	$HL^+ = H^+ + L$, ($L = C_6H_{13}NO$)	7.77	27.4	
Glycerol 2-phosphate	$H_2L = H^+ + HL^-$, ($H_2L = C_3H_9NO_6P$)	1.329	-12.2	-330
	$HL^- = H^+ + L^{2-}$	6.650	-1.85	-212
Glycine	$H_2L^+ = H^+ + HL^\ddagger$, ($HL = C_2H_5NO_2$)	2.351	4.00	-139
	$HL^\ddagger = H^+ + L^-$	9.780	44.2	-57
Glycine amide	$HL^+ = H^+ + L$, ($L = C_2H_6N_2O$)	8.04	42.9	
Glycylglycine	$H_2L^+ = H^+ + HL^\ddagger$, ($HL = C_4H_8N_2O_3$)	3.140	0.11	-128
	$HL^\ddagger = H^+ + L^-$	8.265	43.4	-16
Glycylglycylglycine	$H_2L^+ = H^+ + HL^\ddagger$, ($HL = C_6H_{11}N_3O_4$)	3.224	0.84	
	$HL^\ddagger = H^+ + L^-$	8.090	41.7	
HEPES	$H_2L^+ = H^+ + HL^\ddagger$, ($HL = C_8H_{18}N_2O_4S$)	≈ 3.0		
	$HL^\ddagger = H^+ + L^-$	7.564	20.4	47
HEPPS	$HL^+ = H^+ + L^-$, ($HL = C_6H_{20}N_2O_4S$)	7.957	21.3	48
HEPPSO	$HL^+ = H^+ + L^-$, ($HL = C_9H_{20}N_2O_5S$)	8.042	23.70	47
L-Histidine	$H_3L^{2+} = H^+ + H_2L^+$, ($HL = C_6H_9N_3O_2$)	1.5 ₄	3.6	
	$H_2L^+ = H^+ + HL$	6.07	29.5	176
	$HL = H^+ + L^-$	9.34	43.8	≈ -233
Hydrazine	$H_2L^{2+} = H^+ + HL^\ddagger$, ($L = H_4N_2$)	-0.99	38.1	
	$HL^\ddagger = H^+ + L$	8.02	41.7	
Imidazole	$HL^+ = H^+ + L$, ($L = C_3H_4N_2$)	6.993	36.64	-9
Maleate	$H_2L = H^+ + HL^-$, ($H_2L = C_4H_4O_4$)	1.92	1.1	≈ -21
	$HL^- = H^+ + L^{2-}$	6.27	-3.6	≈ -31
2-Mercaptoethanol	$HL = H^+ + L^-$, ($HL = C_2H_6OS$)	9.7 ₅	26.2	
MES	$HL^\ddagger = H^+ + L^-$, ($HL = C_6H_{13}NO_4S$)	6.270	14.8	5
Methylamine	$HL^+ = H^+ + L$, ($L = CH_5N$)	10.645	55.34	33
2-Methylimidazole	$HL^+ = H^+ + L$, ($L = C_4H_6N_2$)	8.0 ₁	36.8	
MOPS	$HL^\ddagger = H^+ + L^-$, ($HL = C_7H_{15}NO_4S$)	7.184	21.1	25
MOPSO	$H_2L^+ = H^+ + HL^\ddagger$, ($HL = C_7H_{15}NO_5S$)	0.060		
	$HL^\ddagger = H^+ + L^-$	6.90	25.0	≈ 38
Oxalate	$H_2L = H^+ + HL^-$, ($H_2L = C_2H_2O_4$)	1.27	-3.9	≈ -231
	$HL^- = H^+ + L^{2-}$	4.266	7.00	≈ -231
Phosphate	$H_3PO_4 = H^+ + H_2PO_4^-$	2.148	-8.0	-141
	$H_2PO_4^- = H^+ + HPO_4^{2-}$	7.198	3.6	-230
	$HPO_4^{2-} = H^+ + PO_4^{3-}$	12.35	16.0	-242
Phthalate	$H_2L = H^+ + HL^-$, ($H_2L = C_8H_6O_4$)	2.950	-2.70	-91
	$HL^- = H^+ + L^{2-}$	5.408	-2.17	≈ -295
Piperazine	$H_2L^{2+} = H^+ + HL^\ddagger$, ($L = C_4H_{10}N_2$)	5.333	31.11	86
	$HL^\ddagger = H^+ + L$	9.731	42.89	75
PIPER	$HL^\ddagger = H^+ + L^-$, ($HL = C_8H_{18}N_2O_6S_2$)	7.141	11.2	22
POPSO	$HL^\ddagger = H^+ + L^-$, ($HL = C_{10}H_{22}N_2O_8S_2$)	≈ 8.0		
Pyrophosphate	$H_4P_2O_7 = H^+ + H_3P_2O_7^-$	0.83	-9.2	≈ -90
	$H_3P_2O_7^- = H^+ + H_2P_2O_7^{2-}$	2.26	-5.0	≈ -130
	$H_2P_2O_7^{2-} = H^+ + HP_2O_7^{3-}$	6.72	0.5	-136
	$HP_2O_7^{3-} = H^+ + P_2O_7^{4-}$	9.46	1.4	-141
Succinate	$H_2L = H^+ + HL^-$, ($H_2L = C_4H_6O_4$)	4.207	3.0	-121
	$HL^- = H^+ + L^{2-}$	5.636	-0.5	-217
Sulfate	$HSO_4^- = H^+ + SO_4^{2-}$	1.987	-22.4	-258

Buffer	Reaction	pK	$\Delta_f H^\circ$ kJ mol ⁻¹	$\Delta_r C_p^\circ$ J K ⁻¹ mol ⁻¹
Sulfite	$\text{H}_2\text{SO}_3 = \text{H}^+ + \text{HSO}_3^-$	1.857	-17.80	-272
	$\text{HSO}_3^- = \text{H}^+ + \text{SO}_3^{2-}$	7.172	-3.65	-262
TAPS	$\text{HL}^\pm = \text{H}^+ + \text{L}^-, (\text{HL} = \text{C}_7\text{H}_{17}\text{NO}_6\text{S})$	8.44	40.4	15
TAPSO	$\text{HL}^\pm = \text{H}^+ + \text{L}^-, (\text{HL} = \text{C}_7\text{H}_{17}\text{NO}_7\text{S})$	7.635	39.09	-16
L(+)-Tartaric acid	$\text{H}_2\text{L} = \text{H}^+ + \text{HL}^-, (\text{H}_2\text{L} = \text{C}_4\text{H}_6\text{O}_6)$	3.036	3.19	-147
	$\text{HL}^- = \text{H}^+ + \text{L}^{2-}$	4.366	0.93	-218
TES	$\text{HL}^\pm = \text{H}^+ + \text{L}^-, (\text{HL} = \text{C}_6\text{H}_{15}\text{NO}_6\text{S})$	7.550	32.13	0
Tricine	$\text{H}_2\text{L}^+ = \text{H}^+ + \text{HL}^\pm, (\text{HL} = \text{C}_6\text{H}_{13}\text{NO}_5)$	2.023	5.85	-196
	$\text{HL}^\pm = \text{H}^+ + \text{L}^-$	8.135	31.37	-53
Triethanolamine	$\text{HL}^+ = \text{H}^+ + \text{L}, (\text{L} = \text{C}_6\text{H}_{15}\text{NO}_3)$	7.762	33.6	50
Triethylamine	$\text{HL}^+ = \text{H}^+ + \text{L}, (\text{L} = \text{C}_6\text{H}_{15}\text{N})$	10.72	43.13	151
Tris	$\text{HL}^+ = \text{H}^+ + \text{L}, (\text{L} = \text{C}_4\text{H}_{11}\text{NO}_3)$	8.072	47.45	-59